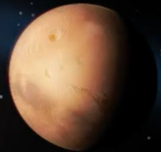


The meteoroid fluence at Mars due to Comet C/2013 A1 (Siding Spring): Two models

Althea Moorhead
NASA Meteoroid Environment Office

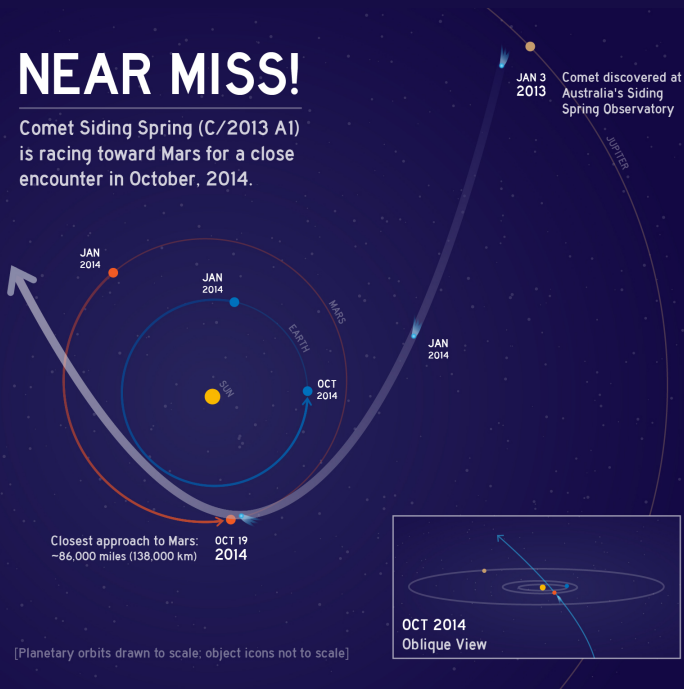
Collaborators:
Paul Wiegert (UWO) & Bill Cooke
Rhiannon Blaauw & Aaron Kingery
Will Yoder & Cameron McCarty



July 2, 2014

NEAR MISS!

Comet Siding Spring (C/2013 A1) is racing toward Mars for a close encounter in October, 2014.



Spherical model

Quantifying the number of $\gtrsim 100$ micron¹ particles:

- 1 Determine brightness.
- 2 Use particle albedo to compute the total particle surface area.
- 3 Use particle size distribution, bulk density to compute number of particles.
- 4 Use r^{-2} spatial distribution to compute the number density.
- 5 Integrate along the trajectory to get fluence.

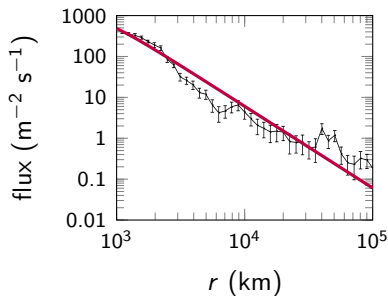
¹100 micron particles are capable of cutting exposed spacecraft wires.

Spherical model

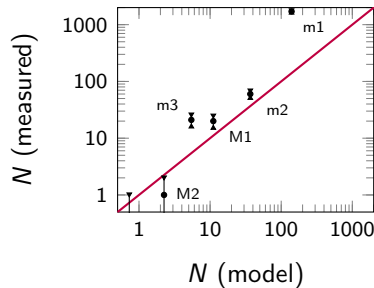
$$\begin{aligned}\sigma_* = & \frac{gh^{-\beta}}{a} \left(\frac{2}{\pi}\right)^{\frac{1}{3}} \left(\frac{\rho}{3}\right)^{\frac{2}{3}} 10^{-0.4(M-1-m_{\odot,1\text{au}})} \text{ au}^2 \\ & \times \left(\frac{3-k}{1-k}\right) \left(\frac{m_{\text{max}}^{(1-k)/3} - m_*^{(1-k)/3}}{m_{\text{max}}^{(3-k)/3} - m_{\text{min}}^{(3-k)/3}}\right) \\ & \times \frac{\cos^{-1}(b/r_c)}{b r_c}\end{aligned}$$

This analytic model can be used to quickly calculate new fluence estimates as comet properties are measured/constrained.

Reproducing *Giotto* and *Stardust* results

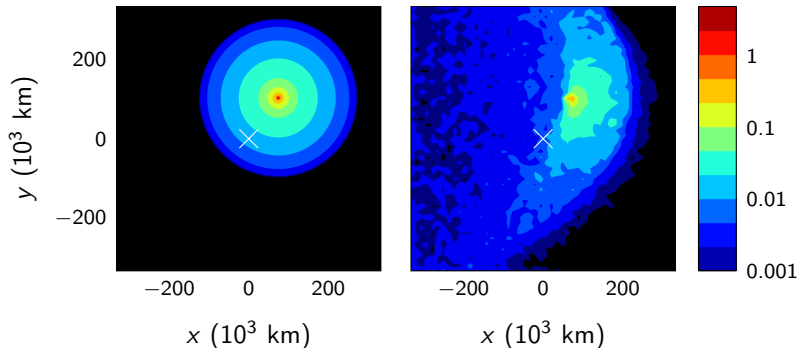


Halley data (Fulle et al., 2000), **our model**



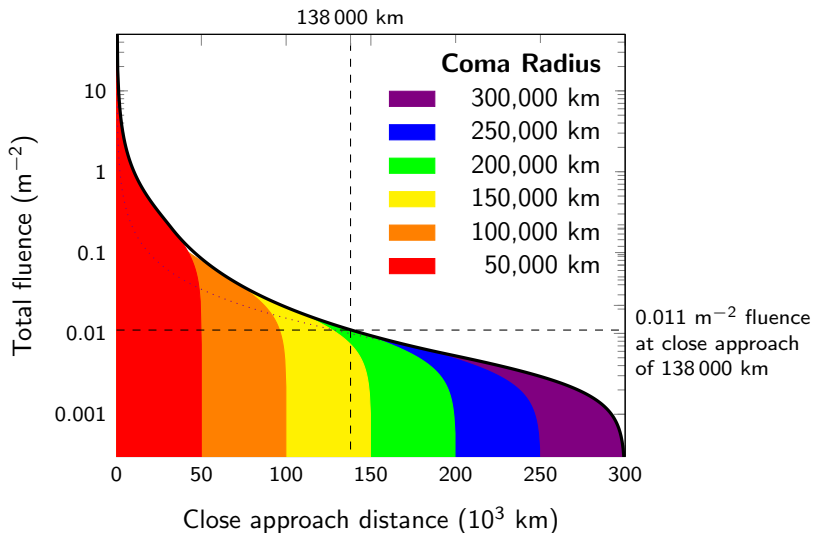
Wild 2 data (Tuzzolino et al., 2004), **our model**

Comparison with simulations



Simulations illustrate (modest) deviance from spherical model due to coma asymmetry and tail.

Dependence on coma size



Quasi-Keplerian model

Trajectory:

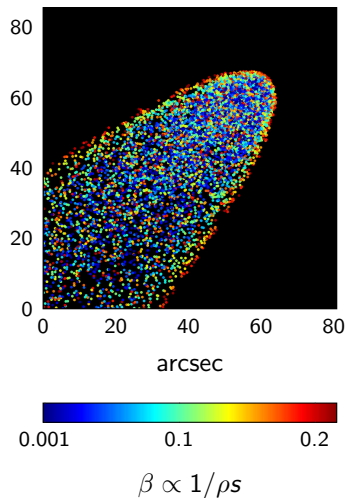
$$v_{ej} = v_0 \beta^{-\mu} r^{-\nu}$$

$$\vec{F} = -\frac{GMm}{r^2} (1 - \beta) \hat{r}$$

Particle distribution:

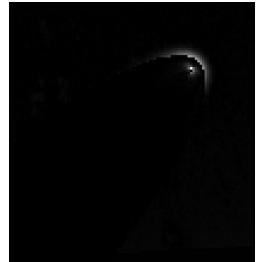
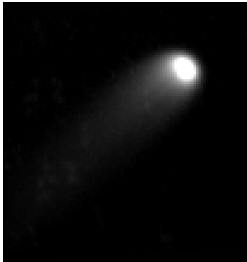
$$\frac{dN}{d\beta} \propto \beta^{\alpha}, \quad \frac{dN}{dr} \propto r^{-\gamma}$$

$$\frac{dN}{dv} \propto 1 - \left(\frac{v/v_{ej} - 1}{f_v} \right)^2$$



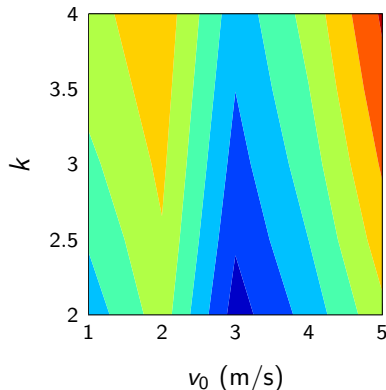
Fit to observations

Using efficient algorithms to solve Kepler's equation (Gooding & Odell, 1988), we can simulate 10^6 particles in seconds:



We use Hubble images (Li et al., 2014) to fit for six parameters.

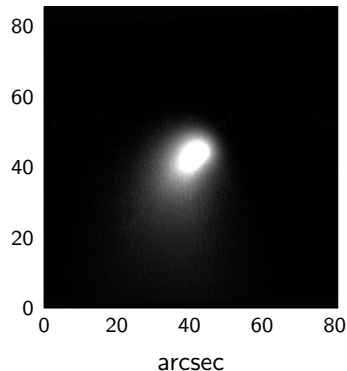
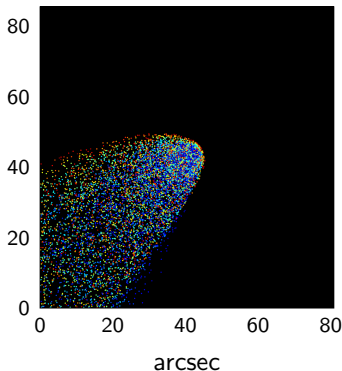
Preliminary results



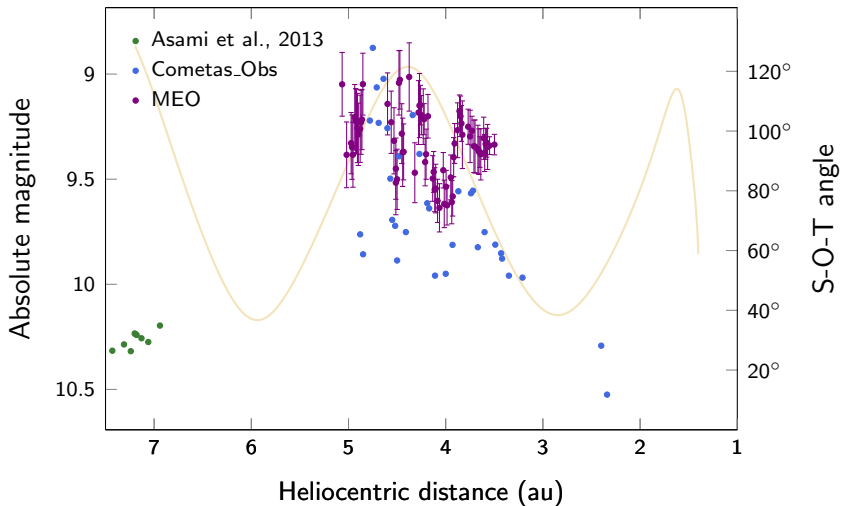
- Used a coarse, 6-d parameter grid
- Simultaneous fitting of all 3 Hubble observations
- Velocities \sim a few m/s
- Flat-to-inverted size distribution favored

Size distribution

Comet's shape in October images requires large particles/small β



Incorporating additional observations



Summary

We've developed two comet models:

- A spherical, analytic model that describes the particle distribution within the coma
 - Provides rough estimate of the meteoroid environment
 - Recreates Halley and Wild 2 particle counts to within an order of magnitude
 - No longer useful for Siding Spring at Mars
- A fast, quasi-Keplerian model that describes the particle distribution in the coma and tail
 - Can be combined with observations to fit for ejection velocity and particle distribution
 - Preliminary fit favors low velocity, flat/inverted size distribution
 - Future work: incorporate ground observations, apply to other monitored comets